Analytic And Computations

Theorems Analytic Computations Computations2 Others



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Theorems for 100.



State Cauchy Integral Formula Formula

$$\frac{n!}{2\pi i} \int_C \frac{f(z)}{(z-z_0)^{n+1}} dz = f^{(n)}(z_0)$$

$$\frac{2\pi i}{n!} \int_C \frac{f(z)}{(z-z_0)^n} dz = f^{(n)}(z_0)$$

$$\int_C \frac{f(z)}{(z-z_0)^n} dz = \frac{2\pi i}{n!} f^{(n)}(z_0)$$

$$\int_C \frac{f(z)}{(z-z_0)^{n+1}} dz = \frac{n!}{2\pi i} f^{(n)}(z_0)$$



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Theorems for 200.



What does Cauchy-Goursat say?

$$f$$
 analytic, C simple, then $\int_C f(z)\,dz=0$ f analytic, C simple, then $\int_C f(z)\,dz>0$

$$f$$
 analytic, C closed, then $\int_C f(z) dz < 0$

f analytic, C simple and closed, then $\int_C f(z) dz = 0$

$$f$$
 continuous, C Jordan, then $\int_C f(z) \, dz = 0$

f bounded, C Jordan, then $\int_C f(z) dz = 0$



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Theorems for 300.

Louville's Theorem states that

Any polynomial has no real roots.

Any polynomial has a real root.

Any polynomial with complex coefficients has a real root.

Any polynomial with complex coefficients has no complex roots.

Any polynomial with complex coefficients has at least a complex root.

Any polynomial with real coefficients has at least one complex root.

none of above



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Theorems for 400



De Moivre formula The roots of $z^n = re^{i\theta}$ are $z_k =$

$$r^{1/k}\left[\cos\left(rac{ heta+2\pi n}{k}
ight)+i\sin\left(rac{ heta+2\pi k}{n}
ight)
ight], \quad k=1,...n$$

$$r^{1/k} \left[\cos \left(\frac{\theta - 2\pi k}{n} \right) + i \sin \left(\frac{\theta + 2\pi k}{n} \right) \right], \quad k = 1, ..., n$$

$$r \left[\cos \left(\frac{\theta + 2\pi n}{k} \right) + i \sin \left(\frac{\theta + 2\pi k}{n} \right) \right], \quad k = 1, ..., n$$

$$r^{1/k} \left[\cos \left(\frac{\theta + 2\pi k}{n} \right) + i \sin \left(\frac{\theta + 2\pi k}{n} \right) \right], \quad k = 0,$$
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none of them



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none of them

$$egin{aligned} v_{ heta} &= ru_r, & u_{ heta} &= -rv_r \\ v_x &= u_y, & v_y &= -u_x \\ v_y &= u_x, & u_x &= -v_y \\ v_x &= v_y, & u_x &= -v_y \\ v_x &= v_y, & u_x &= -u_y \end{aligned}$$

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What does **holomorphic** mean?

Analytic

 $u_{xx} + u_{yy} = 0$

Continuous

Differentiable

 $u_x = v_y$

There is a harmonic conjugate of v none of them

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Analytic for 300.



What does harmonic mean?

Analytic

$$u_x x + u_y y = 0$$

Continuous

Differentiable

 $u_x = v_y$

There is a harmonic conjugate of v none of them

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Analytic for 400.

The circle of radius 5 centered at -i is

$$|z - i|^2 = 5$$

$$|z-i|=25$$

$$|z - i|^2 = 25$$

 $(x - i)^2 + (y - i)^2 = 25$

$$|z+i|=5$$

$$e^{5i} = \theta$$

none of them



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Computations for 100.

A parametrization of the circle of radius 5 centered at -i oriented positively is

$$z = 5e^{i\theta}, \quad \theta \in [0, \pi]$$

$$z = e^{5i\theta}, \quad \theta \in [0, 2\pi]$$

$$z = e^{-5i\theta}, \quad \theta \in [0, \pi]$$

$$z = 5e^{i\theta}, \quad i \in [0, \pi]$$

$$z = 5e^{i\theta}, \quad \pi \in [0, \theta]$$

$$z = 5e^{i\theta}, \quad \theta \in [2\pi, 4\pi]$$

none of them





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For $z=re^{i\Theta},\ \ \Theta\in(-\pi,\pi)$ the Log of z is defined to be

$$\ln r + i\Theta + 2\pi k, \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta - 2\pi k, \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta + \pi k, \quad k \in \mathbb{Z}$$

$$ln r + i(\Theta + \pi k), \quad k \in \mathbb{Z}$$

$$\ln r + 2i(\Theta + \pi k), \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta$$

none of them



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Computations for 300.

For $z=re^{i\Theta},~~\Theta\in(-\pi,\overline{\pi})$ the $\log(z)$ is defined to be

$$\begin{aligned} & \ln r + i(\Theta + 2\pi k), & k \in \mathbb{Z} \\ & \ln r + i\Theta - 2\pi k, & k \in \mathbb{Z} \\ & \ln r + i\Theta + \pi k, & k \in \mathbb{Z} \end{aligned}$$

$$\ln r + i(\Theta + \pi k), \quad k \in \mathbb{Z}$$

 $\ln r + 2i(\Theta + \pi k), \quad k \in \mathbb{Z}$

$$\ln r + i\Theta$$

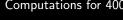
none of them

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Computations for 400.



Which number represents $e^{-3i\pi/2}$?

-i/2

2/ii/1

-i/1

-1/20/2

none of them

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Computations2 for 100.

College

Value of $e^{i\pi/2}$

İ

1

-1

.

none of them

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Computations2 for 200.

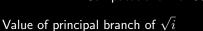
Value of i^{2009}

none of them

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Computations2 for 300.



$$\sqrt{2}/2 - i\sqrt{2}/2$$

i

 $\sqrt{2}/2 + i\sqrt{2}/2$

none of them



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Computations2 for 400.

In hyperbolic functions?

```
\sinh^{2} z + \cosh^{2} z = 1
\sinh^{2} z - \cosh^{2} z = 0
\sinh^{2} z + \cosh^{2} z = 0
-\sinh^{2} z + \cosh^{2} z = 0
-\sinh^{2} z + \cosh^{2} z = 1
none of them
```



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What is a singularity?

A rarity

Something singular

A point where a function is zero

A point for which there is a neighborhood where the function is analytical except at the point

A point where the function vanishes

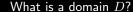
A point where the function is discontinuous none of them

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Others for 200.



Where the function is defined

Where the function is not zero

a set non-empty and connected

They usually tell me

Where I live

none of them



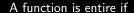
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Others for 300.



it is not broken

it is analytic

it is not rational

it is differentiable everywhere

it is analytic on the complex plane

none of the above



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Others for 400.

What is the Laplace equation?

$$H_{xx}(x,y) + H_{yy}(x,y) = 0$$

$$\int_{C} f dz = 0$$

$$e^{i\theta} = \cos(\theta) + i\sin(\theta)$$

$$\overline{f(z)} = f(\overline{z})$$



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